

**III. A.**

1. The probability that a player wins 5 times in a row is  $\frac{1}{243}$ .

I calculated the answer by using the Rule of Compound Probability involving *and*.

The probability of winning the shell game 1 time is  $\frac{1}{3}$ .

Let  $W$  represent winning the shell game 1 time.

$$P(W) = \frac{1}{3}$$

$$\begin{aligned} P(W, W, W, W, \text{ and } W) &= P(W) \cdot P(W) \cdot P(W) \cdot P(W) \cdot P(W) \\ &= \frac{1}{3} \cdot \frac{1}{3} \cdot \frac{1}{3} \cdot \frac{1}{3} \cdot \frac{1}{3} \\ &= \frac{1}{243} \end{aligned}$$

2. The probability of choosing the same student 5 days in a row is  $\frac{1}{7,962,624}$ .

I calculated the answer by using the Rule of Compound Probability involving *and*.

The probability of choosing the one particular student is  $\frac{1}{24}$ .

Let  $S$  represent choosing a particular student.

$$P(S) = \frac{1}{24}$$

$$\begin{aligned} P(S, S, S, S, \text{ and } S) &= P(S) \cdot P(S) \cdot P(S) \cdot P(S) \cdot P(S) \\ &= \frac{1}{24} \cdot \frac{1}{24} \cdot \frac{1}{24} \cdot \frac{1}{24} \cdot \frac{1}{24} \\ &= \frac{1}{7,962,624} \end{aligned}$$

3. The probability that the first two spinners land on 1 is  $\frac{1}{24}$ .

I calculated the answer by using the Rule of Compound Probability involving *and*.

The probability of the 1st spinner landing on 1 is  $\frac{1}{6}$ .

$$P(1 \text{ on 1st spinner}) = \frac{1}{6}$$

The probability of the 2nd spinner landing on 1 is  $\frac{1}{4}$ .

$$P(1 \text{ on 2nd spinner}) = \frac{1}{4}$$

The probability of the 3rd spinner landing on any number is  $\frac{12}{12}$ , or 1.

$$P(\text{any number on 3rd spinner}) = 1$$

I don't have to include the probability of the 3rd spin in my calculation because multiplying by 1 will not affect the final answer.

$$\begin{aligned} P(1 \text{ on 1st spinner and } 1 \text{ on 2nd spinner}) &= P(1 \text{ on 1st spinner}) \cdot P(1 \text{ on 2nd spinner}) \\ &= \frac{1}{6} \cdot \frac{1}{4} \\ &= \frac{1}{24} \end{aligned}$$

4. The probability of choosing a block labeled W from the second set is  $\frac{1}{4}$ .

I calculated the answer by using the Rule of Compound Probability involving *and*.

The probability of choosing any block from the first set is  $\frac{12}{12}$ , or 1.

$$P(\text{any block 1st}) = 1$$

The probability of choosing a block labeled W from the second set is  $\frac{3}{12}$ , or  $\frac{1}{4}$ .

$$P(W \text{ 2nd}) = \frac{1}{4}$$

I don't have to include the probability of any block 1st in my calculation because multiplying by 1 will not affect the final answer. So, the final answer is  $P(W \text{ 2nd}) = \frac{1}{4}$ .

5. The probability of choosing two marbles with stripes is  $\frac{7}{34}$ .

I calculated the answer by using the Rule of Compound Probability involving *and*.

The probability of choosing a marble with stripes from the 1st set is  $\frac{7}{17}$ .

Let  $A$  represent choosing a marble with stripes from the 1st set.

$$P(A) = \frac{7}{17}$$

The probability of choosing a marble with stripes from the 2nd set is  $\frac{9}{18}$ , or  $\frac{1}{2}$ .

Let  $B$  represent choosing a marble with stripes from the 2nd set.

$$P(B) = \frac{1}{2}$$

$$P(A \text{ and } B) = P(A) \cdot P(B)$$

$$= \frac{7}{17} \cdot \frac{1}{2}$$

$$= \frac{7}{34}$$

6. The probability that a player wins 5 times in a row is  $\frac{1}{9,765,625}$ .

I calculated the answer by using the Rule of Compound Probability involving *and*.

The probability of me or my friend winning the prize 1 time is  $\frac{2}{50}$ , or  $\frac{1}{25}$ .

Let  $W$  represent me or my friend winning the prize 1 time.

$$P(W) = \frac{1}{25}$$

$$P(W, W, W, W, \text{ and } W) = P(W) \cdot P(W) \cdot P(W) \cdot P(W) \cdot P(W)$$

$$= \frac{1}{25} \cdot \frac{1}{25} \cdot \frac{1}{25} \cdot \frac{1}{25} \cdot \frac{1}{25}$$

$$= \frac{1}{9,765,625}$$

### III. B.

1. The probability of choosing a block labeled with a 7 or a block labeled with a 6 is  $\frac{11}{32}$ .

2. The probability of choosing a rotten apple or a rotten orange is  $\frac{41}{432}$ .

3. The probability of a one on the 1st roll or a one on the 2nd roll is  $\frac{11}{36}$ .
4. The probability of landing on a number greater than 9 on the 1st spin or a number less than 6 on the 2nd spin is  $\frac{9}{16}$ .
5. The probability that the student chosen from the math class or the student chosen from the history class is in the band is  $\frac{15}{32}$ .
6. The probability of choosing a pyramid from the shaded set or a cylinder from the unshaded set is  $\frac{79}{169}$ .

### III. C.

1. The probability of choosing a 2 first and a 3 second is  $\frac{1}{9}$ .
2. The probability of choosing a green marble first, a red marble second, and a blue marble third is  $\frac{96}{15,625}$ .
3. The probability of choosing a triangle first or a square second is  $\frac{4}{9}$ .
4. The probability of choosing an A block first or a D block second is  $\frac{29}{64}$ .
5. The probability of choosing a quarter first or a dime second is  $\frac{49}{121}$ .
6. The probability of choosing a green block first, a yellow block second, and a blue block third is  $\frac{9}{2662}$ .

### IV. A.

1. The probability of choosing all 4 aces is  $\frac{1}{270,725}$ .

I calculated the answer by using the Rule of Compound Probability involving *and*.

The probability of choosing an ace first is  $\frac{4}{52}$ , or  $\frac{1}{13}$ .

The probability of choosing an ace second is  $\frac{3}{51}$ , or  $\frac{1}{17}$ .

The probability of choosing an ace third is  $\frac{2}{50}$ , or  $\frac{1}{25}$ .

The probability of choosing an ace fourth is  $\frac{1}{49}$ .

$$\begin{aligned}
 P(\text{ace 1st, ace 2nd, ace 3rd, and ace 4th}) &= P(\text{ace 1st}) \cdot P(\text{ace 2nd}) \cdot P(\text{ace 3rd}) \cdot P(\text{ace 4th}) \\
 &= \frac{1}{13} \cdot \frac{1}{17} \cdot \frac{1}{25} \cdot \frac{1}{49} \\
 &= \frac{1}{270,725}
 \end{aligned}$$

2. The probability that the first two ribbons will be yellow is  $\frac{1}{51}$ .

I calculated the answer by using the Rule of Compound Probability involving *and*.

The probability of choosing a yellow ribbon 1st is  $\frac{3}{18}$ , or  $\frac{1}{6}$ .

The probability of choosing a yellow ribbon 2nd is  $\frac{2}{17}$ .

The probability of choosing any ribbon 3rd is  $\frac{16}{16}$ , or 1.

I don't have to include the probability of choosing any ribbon 3rd in my calculation because multiplying by 1 will not affect the final answer.

$$\begin{aligned}
 P(\text{yellow 1st and yellow 2nd}) &= P(\text{yellow 1st}) \cdot P(\text{yellow 2nd}) \\
 &= \frac{1}{6} \cdot \frac{2}{17} \\
 &= \frac{1}{51}
 \end{aligned}$$

3. The probability of choosing 4 discs in alphabetical order is  $\frac{9}{1820}$ .

I calculated the answer by using the Rule of Compound Probability involving *and*.

The probability of choosing a disc with an A 1st is  $\frac{6}{16}$ , or  $\frac{3}{8}$ .

The probability of choosing a disc with a B 2nd is  $\frac{3}{15}$ , or  $\frac{1}{5}$ .

The probability of choosing a disc with a C 3rd is  $\frac{3}{14}$ .

The probability of choosing a disc with a D 4th is  $\frac{4}{13}$ .

$$\begin{aligned}
 P(\text{A 1st, B 2nd, C 3rd, and D 4th}) &= P(\text{A 1st}) \cdot P(\text{B 2nd}) \cdot P(\text{C 3rd}) \cdot P(\text{D 4th}) \\
 &= \frac{3}{8} \cdot \frac{1}{5} \cdot \frac{3}{14} \cdot \frac{4}{13} \\
 &= \frac{36}{7280} \\
 &= \frac{9}{1820}
 \end{aligned}$$

4. The probability of Evan choosing a quarter 1st is  $\frac{2}{7}$ .

I calculated the answer by using the Rule of Compound Probability involving *and*.

The probability of choosing a quarter 1st  $\frac{6}{21}$  is, or  $\frac{2}{7}$ .

The probability of choosing any coin 2nd is  $\frac{20}{20}$ , or 1.

The probability of choosing any coin 3rd is  $\frac{19}{19}$ , or 1.

I don't have to include the probability of choosing any coin 2nd or the probability of choosing any coin 3rd in my calculation because multiplying by 1 will not affect the final answer. So, the probability of Evan choosing a quarter 1st is  $\frac{2}{7}$ .

5. The probability of choosing 4 students with birthdays in June, July, or August is  $\frac{2}{325}$ .

I calculated the answer by using the Rule of Compound Probability involving "and".

The probability of the 1st student having a birthday in June, July, or August is  $\frac{9}{28}$ .

The probability of the 2nd student having a birthday in June, July, or August is  $\frac{8}{27}$ .

The probability of the 3rd student having a birthday in June, July, or August is  $\frac{7}{26}$ .

The probability of the 4th student having a birthday in June, July, or August is  $\frac{6}{25}$ .

Let  $B$  represent choosing a student with a birthday in June, July, or August.

$$\begin{aligned}
 P(\text{B 1st, B 2nd, B 3rd, and B 4th}) &= P(\text{B 1st}) \cdot P(\text{B 2nd}) \cdot P(\text{B 3rd}) \cdot P(\text{B 4th}) \\
 &= \frac{9}{28} \cdot \frac{8}{27} \cdot \frac{7}{26} \cdot \frac{6}{25} \\
 &= \frac{3024}{491,400} \\
 &= \frac{2}{325}
 \end{aligned}$$

6. The probability of the 1st cards not having a 9 as one of its digits and the 2nd and 3rd cards having a 9 as one of their digits is  $\frac{41}{7095}$ .

I calculated the answer by using the Rule of Compound Probability involving *and*.

The probability that the 1st number does not have a 9 as one of its digits is  $\frac{41}{45}$ .

The probability that the 2nd number has a 9 as one of its digits is  $\frac{4}{44}$ .

The probability that the 3rd number has a 9 as one of its digits is  $\frac{3}{43}$ .

Let  $N$  represent choosing a card that has a 9 as one of its digits.

$$\begin{aligned}
 P(\text{not } N \text{ 1st and } N \text{ 2nd and } N \text{ 3rd}) &= P(\text{not } N \text{ 1st}) \cdot P(N \text{ 2nd}) \cdot P(N \text{ 3rd}) \\
 &= \frac{41}{45} \cdot \frac{4}{44} \cdot \frac{3}{43} \\
 &= \frac{492}{85,140} \\
 &= \frac{41}{7095}
 \end{aligned}$$

#### IV. B.

1. The probability of choosing a blue sock first or a green sock second is  $\frac{83}{190}$ .
2. The probability of choosing a cube with a 2 first or a cube with a 3 second is  $\frac{32}{105}$ .
3. The probability that I will be chosen first or my friend will be chosen second is  $\frac{27}{574}$ .
4. The probability that the first ball has stars or the second ball has stripes is  $\frac{109}{190}$ .
5. The probability of choosing an ace first or a King second is  $\frac{98}{663}$ .
6. The probability of a favorite song first or a favorite song second is  $\frac{94}{325}$ .

#### IV. C.

1. The probability of choosing a pyramid first, cube second, and cylinder third is  $\frac{9}{220}$ .
2. The probability of choosing a pear first or an orange second is  $\frac{29}{66}$ .
3. The probability of choosing a white ball first or a shaded ball second is  $\frac{11}{15}$ .
4. The probability that the first student will draw an A and the second student will draw a B is  $\frac{137}{276}$ .
5. The probability of choosing a black sock first and a black sock second is  $\frac{14}{95}$ .
6. The probability of choosing a J block first or a K block second is  $\frac{53}{91}$ .
7. The probability of choosing a numbered card first or a King second is  $\frac{158}{221}$ .
8. The probability of choosing a blue t-shirt first and another blue t-shirt second is  $\frac{1}{11}$ .